

Winning by Default: Why is There So Little Competition in Government Procurement?

Karam Kang and Robert A. Miller

Carnegie Mellon University

March 2017

Procurement and Little Competition

- Ubiquitous problem to find a suitable contractor from a small pool of contenders
 - Commercially unavailable goods or services
 - Negotiation of price and contract terms
- US federal procurement (FY 2013):
 - Median number of bids is one
 - \$0.2 trillion (44%) paid for contracts with a single bidder
 - Most large, non-repetitive contracts are negotiated

Why Little Competition?

- Benefits and costs of attracting/considering another contractor
 - Lower contract price due to competition
 - Administration and search cost
 - Capture and corruption
- Contract negotiations during the selection process are relevant
- Goal: To quantify the factors determining competition under contract negotiation

What This Paper Does

- Develop a principal-agent model where the procurer
 - ① Chooses the extent of competition
 - ② Negotiates the contract terms
- Identify and estimate the model using the data on the Federal IT/telecommunications service procurement contracts of FY 2004-2012
- Conduct counter-factual analyses of the estimated model to quantify the factors determining competition

Preview of the Results

- Negotiations substantially reduce the informational asymmetry between a procurer and contractors:
 - $\mathbb{E}(\text{price}|\text{negotiation, one bidder}) \approx \mathbb{E}(\text{price}|\text{auction, two bidders})$
 - Cost savings from negotiations (as opposed to a standard first-price auction): \$63,500 per \$1-million contract
- Allowing discretion to contracting officers reduces government cost

Literature Review

- Nonstandard auctions: *Negotiations vs. auctions* - Bajari, McMillan, and Tadelis (2008); *Preference program* - Krasnokutskaya and Seim (2011), Athey, Coey, and Levin (2013); *Scoring* - Asker and Cantillon (2010); *Endogenous Entry* - Li and Zheng (2009)
- Corruption and regulatory capture: *Active vs. passive waste* - Bandiera, Prat, Valletti (2009); *Discretion* - Coviello, Guglielmo, and Spagnolo (2014)
- Auctioning incentive contracts: Laffont and Tirole (1987), McAfee and McMillan (1987), Riordan and Sappington (1987)
- Price adjustments and contract renegotiation: Bajari, Houghton, and Tadelis (2014), Kosmopoulou and Zhou (2014)
- Identification of adverse selection model: Perrigne and Vuong (2011)

Today's Talk

- ① Institutional background and descriptive statistics
- ② Model of procurement with negotiations
- ③ Nonparametric identification of the model given our data
- ④ Estimation results

Data

- Source: Federal Procurement Data System - Next Generation
- For each procurement project, we observe
 - ① Competitive or noncompetitive (and why)
 - ② Number of bids
 - ③ History of price and duration changes
 - ④ Product/service code, agency, and location
- IT/telecommunications service contracts of FY 2004-2012:
 - ① With specified quantity and delivery schedule
 - ② Of a large size (\$300K–\$5M) and commercially unavailable

Extent of Competition

| Extent of competition | Number | Size (\$M) |
|-------------------------------|-----------|------------|
| Limited/no competition | 1,952 | 1.52 |
| Unavailable for competition | 925 (47%) | 1.30 |
| Set-asides for small business | 215 (11%) | 1.63 |
| Not competed by discretion | 812 (42%) | 1.75 |
| Full and open competition | 753 | 1.30 |
| One bid | 274 (36%) | 1.15 |
| Two bids | 121 (16%) | 1.29 |
| Three bids | 197 (26%) | 1.27 |
| More than three bids | 161 (21%) | 1.61 |

Note: All definitive IT/telecommunications contracts for commercially unavailable services of FY 2004-2012, a large size (\$0.3–5 million): 2,705 contracts, \$3.8 billion (CPI-adjusted, 2010 dollars) in total.

Extent of Competition

- Reasons for no competition by discretion:
 - Only one source available (brand, patent, etc.; 56%), follow-on contract (17%), urgency (8%), other/unspecified (national security, public interest, etc.; 19%)
- Costly efforts for bids:
 - Information exchanges with potential contractors prior to issuing a RFP (pre-solicitation notices, industry conferences, public hearings, market research, one-on-one meetings)

Contract Negotiation

- A contract awarded using other than sealed bidding procedures is defined as a *negotiated* contract (FAR 15.000)
- Focus attention to the following two types of negotiated contracts
 - ① Noncompetitive: Discretionary (42% of those noncompeted)
 - ② Competitive: Negotiated proposal solicitation (56% of those competed)

Contract Price and Duration Changes

- Two types of contract price and duration changes:
 - ① *Unilateral*
 - No requirement for both parties' agreement; i.e., following the initial contract terms
 - Exercise an option, termination, administrative actions
 - ② *Bilateral*
 - Requirement for both parties' agreement; i.e., renegotiation
 - Additional work, supplemental agreement for work within scope, change order

▶ More

Price and Duration by Competition

| | Noncompetitive | Competitive | |
|------------------------------------|----------------|-------------|-------------|
| | | 1 Bid | 2+ Bids |
| Number of Observations | 652 | 83 | 227 |
| Total payment (\$M) | 1.20 (1.12) | 1.20 (1.11) | 1.45 (1.17) |
| Fraction of price changes | | | |
| Unilateral | 0.58 | 0.60 | 0.54 |
| Bilateral | 0.38 | 0.35 | 0.35 |
| Amount of price changes (\$M) | | | |
| Unilateral | 0.35 (0.63) | 0.35 (0.62) | 0.39 (0.74) |
| Bilateral | 0.19 (0.51) | 0.18 (0.45) | 0.16 (0.53) |
| Total duration (years) | 2.08 (1.74) | 2.55 (1.92) | 2.24 (1.80) |
| Length of duration changes (years) | | | |
| Unilateral | 0.63 (1.23) | 0.96 (1.48) | 0.77 (1.39) |
| Bilateral | 0.32 (0.85) | 0.27 (0.73) | 0.27 (0.90) |

Note: Final sample of 962 obs.; standard deviations are in parentheses.

Competition and Military Contracts

| | Noncompetitive | One Bid | Num. of Bids |
|-------------------------|----------------------|-----------------------|------------------|
| Military agency | 0.144*** (0.0417) | 0.120*** (0.0258) | 1.182 (1.244) |
| Log(Duration, in days) | | -0.0263** (0.0126) | 0.764 (1.236) |
| Base price (\$K) | | 0.711*** (0.167) | 5.867 (7.537) |
| Product/service code FE | Yes | Yes | Yes |
| State, year, month FE | Yes | Yes | Yes |
| N | 962 | 962 | 310 |
| R^2 | 0.182 | 0.193 | 0.319 |

Note: All contracts in the sample, except the last specification for competitive contracts only; standard errors are clustered at the product/service code level, and provided in parentheses; * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$. *Military agencies* include the Departments of State, Defense, and Homeland Security.

Unilateral Price and Duration Changes

| | Unilateral price change (\$K) | | |
|--|-------------------------------|---------------------|---------------------|
| Unilateral duration change/Base duration | 70.77*** (15.61) | 81.19*** (18.78) | 81.74*** (18.41) |
| Base duration (days) | | 0.203** (0.0805) | 0.208** (0.0791) |
| Base price (\$K) | | 0.0938* (0.0549) | 0.0891 (0.0558) |
| Noncompetitive | | -104.6 (175.6) | -6.546 (125.8) |
| One bid | | -63.77 (145.3) | |
| Log (number of bids) | | | 143.6 (90.94) |
| Product/service code FE | Yes | Yes | Yes |
| Agency, state, year, month FE | No | Yes | Yes |
| N | 554 | 554 | 554 |
| R ² | 0.106 | 0.412 | 0.417 |

Note: Contracts with unilateral price changes in the sample; standard errors are clustered at the product/service code level, and provided in parentheses; * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$.

Key Features of the Model

- ① Procurer chooses whether to solicit bids or not
 - Cost reduction from competition, quality (“only one source”), administrative cost of formal solicitation process (“urgency”), corruption
- ② She chooses the level of effort for attracting bidders
 - More effort (various exchanges of information prior to a RFP) leads to more bids, but at a higher cost
- ③ Given the bidders, she offers a menu of contracts
 - We model the individual, simultaneous negotiation as an adverse selection model with multiple agents

Timeline and Choices

- 1 Procurer chooses whether to solicit bids
- 2 If soliciting bids, she chooses the level of effort to attract bidders, determining the distribution of the number of bidders
- 3 Given the number of bidders, the procurer offers a menu of contracts
- 4 Bidders choose a contract from the menu
- 5 Given the contract choices, the procurer chooses a winner
- 6 Based on the project outcomes, the final payment is determined

Information

- A model of hidden information with two cost types of contractors
 - Contractors know their own cost type, while procurer does not
 - Low-cost contractor: $\alpha + \epsilon$
 - High-cost contractor: $\alpha + \beta + \epsilon$ with $\beta > 0$
- *Cost shock*(ϵ) and *signal*(s) are realized and observed by both parties
 - Cost shock is independent of cost type
 - Signal depends on contractors' cost type

Procurer's Choices and Payoff

- Procurer decides
 - ① Whether to solicit bids
 - ② Bidder arrival rate λ : Number of *extra* bidders $\sim \text{Poisson}(\lambda)$
 - ③ Menu of contracts and the winner
- Procurer's total cost includes
 - ① Payment to the contractors
 - ② Bid processing cost ($\kappa\lambda$)
 - ③ Formal solicitation procedure cost (η)

Contractors' Payoff and Choice

- Contractors choose a contract from a given menu
- A typical contract consists of base price (p) and ex-post price adjustment (Δ)
- Contractors consider the expected profit from procurement:

$$\underbrace{p - (\alpha + \beta)}_{\text{deterministic payoff}} + \underbrace{\mathbb{E}[\psi(\Delta - \epsilon)]}_{\text{stochastic payoff}},$$

where $\psi' > 0$, $\psi'' < 0$, $\psi(0) = 0$, and $\psi'(0) = 1$

- Liquidity concerns, or the cost of working capital, lead the winning contractor to discount the variable part of the payoff, and enlarge unanticipated cost adjustments [▶ More](#)

Equilibrium Menu of Contracts

- We characterize a menu of two contracts (*fixed* vs. *variable*) that induces a truth-telling Bayesian Nash equilibrium
 - ① Both contracts allow *bilateral* changes to insure cost shock
 - ② Only variable contracts allow *unilateral* changes, contingent on signal
- When the number of bids is small, the expected transfer given this scheme is smaller than that of a standard auction

Equilibrium Menu of Contracts: A Cut-down Problem

- Given ex-ante symmetric n bidders, procurer minimizes

$$\underbrace{(1 - (1 - \pi)^n)}_{\text{Pr. of receiving at least 1 eff. bid}} \underline{p}_n + (1 - \pi)^n (\bar{p} + \int q(s) \bar{f}(s) ds)$$

subject to

$$\bar{p} + \int \psi[q(s)] \bar{f}(s) ds - (\alpha + \beta) \geq 0 \quad (\text{IR: High-cost})$$

$$\underline{\phi}_n \{ \underline{p}_n - \alpha \} \geq \bar{\phi}_n \left\{ \bar{p} + \int \psi[q(s)] \underline{f}(s) ds - \alpha \right\} \quad (\text{IC: Low-cost})$$

Equilibrium Menu of Contracts: Characterization

- Procurer offers a menu of two contracts that induces a truth-telling Bayesian Nash equilibrium

- ① Fixed-price contract: $\underline{p}_n + \epsilon$, where

$$\underline{p}_n = \alpha + \frac{\pi(1-\pi)^{n-1}}{1-(1-\pi)^n} \left\{ \beta - \int \psi[q(s)] [\bar{f}(s) - \underline{f}(s)] ds \right\}.$$

- ② Variable-price contract: $\bar{p} + q(s) + \epsilon$, where

$$\bar{p} = \alpha + \beta - \int \psi[q(s)] \bar{f}(s) ds,$$

$$\psi'[q(s)] [1 - \pi \underline{f}(s) / \bar{f}(s)] = 1 - \pi.$$

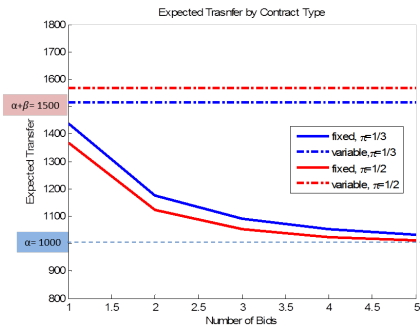
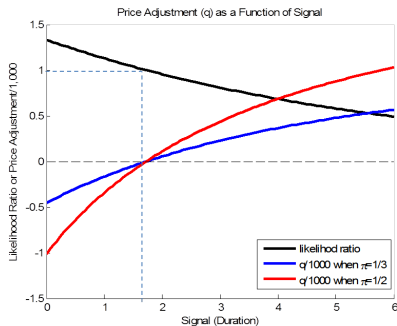
Comparative Statics: Variable-price Contracts

- There is a trade-off between *extracting more rents from the low-cost contractor* vs. *paying a higher risk premium to the high-cost contractor to maintain IR and IC*:

$$\psi'[q(s)] [1 - \pi \underline{f}(s)/\bar{f}(s)] = 1 - \pi.$$

- ❶ If $\underline{f}(s) = \bar{f}(s)$, then $\psi'[q(s)] = 1$, or $q(s) = 0$.
- ❷ If $\underline{f}(s) < \bar{f}(s)$, then $\psi'[q(s)] < 1$, or $q(s) > 0$.
- ❸ If $\underline{f}(s) > \bar{f}(s)$, then $\psi'[q(s)] > 1$, or $q(s) < 0$.

Trade-off: *Informational rents* vs. *Risk premium*



- Likelihood ratio: Likelihood that a contractor is the low-cost type given signal
- q : Ex-post price adjustment due to signal
- π : Proportion of low-cost contractors
- α : Expected project cost for low-cost contractors
- β : Expected *extra* project cost for high-cost contractors

Identification

- We observe the joint distribution of (entry restrictions, number of bids, contract type, base price, price adjustment, and signals).
- We treat π (the proportion of low-cost contractors) as an unobserved heterogeneity and allow other primitives of the model to vary with π .
 - ① Project costs: $\alpha(\pi)$ (for low-cost contractors) and $\beta(\pi)$ (extra costs for high-cost contractors)
 - ② Bid cost: $\kappa(\pi)$
 - ③ We assume that π , signals (s), and direct cost of entry restriction (η) are mutually independent.
- We identify (i) the distribution of π , signal, and η ; (ii) project costs and bid cost as functions of π ; and (iii) liquidity cost function.

Identification

- In this talk, we focus on the case that the ex-post price adjustment ($q(s; \pi)$) for any given (s, π) is an interior solution.
- For identification, we exploit the following monotone relationship between π and contracts:
 - ① If $q(s; \pi)$ is an interior solution, then $\partial |q(s; \pi)| / \partial \pi > 0$.
 - ② With project costs non-increasing in π , $\partial \underline{p}_n(\pi) / \partial \pi < 0$.
 - ③ With a further assumption on $\partial(\alpha + \beta) / \partial \pi$, $\partial \bar{p}(\pi) / \partial \pi < 0$.

Identification: Sketch of the Proof (1/4)

- Given the separating equilibrium, the signal distribution of fixed contracts is $\underline{f}(s)$, and that of variable contracts is $\bar{f}(s)$.
- By monotonicity, there exists a one-to-one mapping between the likelihood ratio $l(s) \equiv \underline{f}(s)/\bar{f}(s)$ and (\bar{p}, q) , denoted by $l^*(\bar{p}, q)$.

$$\psi''(q) = \left[\frac{1 - \psi'(q)}{1 - l^*(q, \bar{p})} \right] \psi'(q) \frac{\partial l^*(q, \bar{p})}{\partial q}.$$

- This first-order ODE is derived from the FOC wrt q .
- We can solve $\psi(\cdot)$ uniquely using $\psi'(0) = 1$ and $\psi(0) = 0$.

Identification: Sketch of the Proof (2/4)

- Since $\psi(\cdot)$ is identified, so is π corresponding to each variable contract (\bar{p}, q, s) defined through the FOC by:

$$\pi_{q,s} \equiv \frac{1 - \psi' [q(s)]}{1 - I(s) \psi' [q(s)]}.$$

- Given the above equation, we identify the distribution of π for variable contracts conditional on number of bids (n) and competition (c), $f_{\pi|v,n,c}(\pi|1, n, c)$.
- Using the theoretical prediction on the probability of having a fixed-contract conditional on (π, n) , [▶ More](#)

$$f_{\pi|v,n,c}(\pi|0, n, c) = \frac{[1 - (1 - \pi)^n] \Pr(v = 1|n, c)}{(1 - \pi)^n \Pr(v = 0|n, c)} f_{\pi|v,n,c}(\pi|1, n, c).$$

Identification: Sketch of the Proof (3/4)

- Using the monotonicity between the fixed-price (\underline{p}) and π :

$$\underline{p}_n^*(\pi, c) = G_{\underline{p}_n|c}^{-1} \left(\int_{\pi}^{\pi_{\max}} f_{\pi|c,n,v}(x|c, n, 0) dx \middle| c \right).$$

- Project costs are identified from the equilibrium characterization.

$$\alpha(\pi) = \frac{1 - (1 - \pi)^n}{1 - (1 - \pi)^{n-1}} \underline{p}_n^*(\pi, c) - \frac{\pi (1 - \pi)^{n-1}}{1 - (1 - \pi)^{n-1}} \underline{p}_1^*(\pi, c),$$

$$\beta(\pi) = \bar{p}^* \left(h \left[\frac{1 - \pi}{1 - \pi l(s)} \right], s \right) + \int \psi \left(h \left[\frac{1 - \pi}{1 - \pi l(t)} \right] \right) \bar{f}(t) dt - \alpha(\pi),$$

where $\bar{p}^*(q, s)$ is identified directly from data.

Identification: Sketch of the Proof (4/4)

- Bid solicitation costs, $\kappa(\pi)$, are identified from the FOC regarding the extra bid arrival rate, $\lambda(\pi)$:

$$\lambda(\pi) = \sum_{n=0}^{\infty} \frac{nf_{\pi,n|c}(\pi, n+1|1)}{f_{\pi|c}(\pi|1)},$$

If $\lambda(\pi) > 0$,

$$\kappa(\pi) = \pi \Gamma(\pi) \exp[-\pi \lambda(\pi)],$$

where $\Gamma(\cdot)$ is an identified function of π .

- Probability of entry restrictions conditional on π help identify the distribution of η . The optimal entry restriction rule is

$$\eta \leq \frac{\kappa(\pi)}{\pi} \{1 + \ln(\pi) + \ln[\Gamma(\pi)] - \ln[\kappa(\pi)]\} - \Gamma(\pi).$$

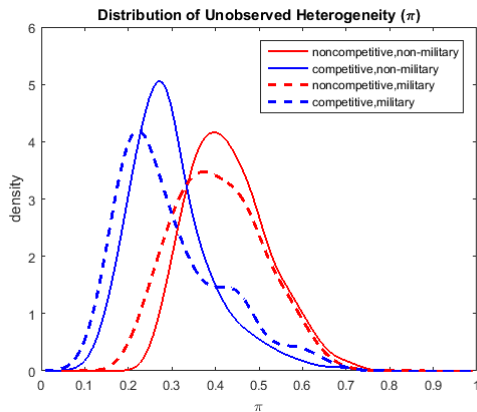
Estimation

- Since the number of observations is 962 (which is small for a nonparametric analysis), we estimate a parametric model using a simulated GMM estimator.
- Moment conditions are motivated by the identification arguments:
- In our estimated model,
 - ① Signals: Duration changes *NOT* attributed to bilateral modifications
 - ② Cost shocks: Price changes attributed to bilateral modifications

Model Fit

| | Observed | Predicted |
|---|----------|-----------|
| Probability of | | |
| Entry restriction | 0.6778 | 0.7374 |
| One bid conditioning on competition | 0.2677 | 0.3062 |
| Up to two bids conditioning on competition | 0.4258 | 0.5209 |
| Up to five bids conditioning on competition | 0.8516 | 0.9162 |
| Fixed contracts conditioning on entry restriction | 0.4156 | 0.4307 |
| Fixed contracts conditioning on one bid | 0.3976 | 0.4254 |
| Fixed contracts conditioning on up to two bids | 0.4091 | 0.4561 |
| Fixed contracts conditioning on up to five bids | 0.4621 | 0.5594 |
| Average transfer (\$M) of fixed contracts | | |
| Conditioning on entry restriction | 0.8256 | 0.7578 |
| Conditioning on competition | 1.1869 | 1.0863 |
| Average transfer (\$M) of variable contracts | | |
| Conditioning on entry restriction | 1.1397 | 1.0951 |
| Conditioning on competition | 1.2322 | 1.0153 |

Estimated Endogenous π Distribution



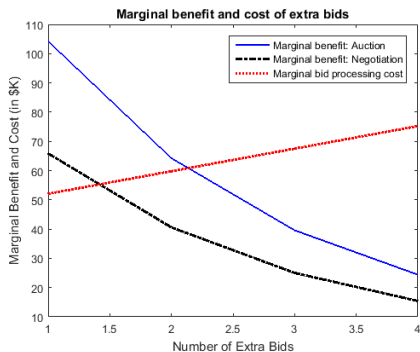
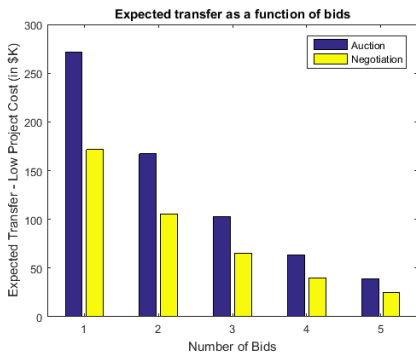
Why So Little Competition? (1/3)

- For a project with $\pi = 0.35$,

| (in \$K) | Non-military | | Military | |
|--|--------------|-------|----------|-------|
| | Estimate | SE | Estimate | SE |
| Low project cost (α) | 958.33 | 40.44 | 985.03 | 46.59 |
| Project cost difference (β) | 294.11 | 33.86 | 254.48 | 33.95 |
| Per-bidder bid cost (κ) | 46.49 | 8.09 | 46.49 | 8.09 |
| Entry restriction benefit ($\mathbb{E}(\eta)$) | 20.50 | 4.77 | 33.60 | 7.56 |

- Average direct benefits from restricting entry: [\$30,160,\$30,929] per noncompetitive contract
- Average bid costs: [\$60,271,\$63,052] per competitive contract

Why So Little Competition? (2/3)



Why So Little Competition? (3/3)

- ❶ 50% decrease in the the per-bidder cost of attracting bids
- ❷ 50% decrease in the benefits from imposing entry restrictions
- ❸ Competition is required for all contracts
- ❹ At least two bids are mandatory
- ❺ First-price sealed-bid auction

| | Base | (1) | (2) | (3) | (4) | (5) |
|----------------------------------|---------|--------|--------|--------|--------|--------|
| Probability of restricting entry | 0.74 | -0.30 | -0.39 | -0.74 | -0.74 | -0.29 |
| Average number of bids | 1.48 | +1.18 | +0.22 | +0.31 | +1.31 | +0.67 |
| Probability of fixed contracts | 0.47 | +0.14 | +0.04 | +0.06 | +0.25 | +0.53 |
| Average costs (\$K) | | | | | | |
| Transfer | 1027.38 | -46.20 | -11.85 | -16.76 | -63.27 | +32.08 |
| Bid costs | 16.19 | +21.95 | +9.89 | +14.31 | +74.94 | +31.44 |
| Entry restriction costs | -22.52 | +7.50 | +16.82 | +22.52 | +22.52 | +6.69 |
| Efficiency loss costs | 3.37 | -1.20 | -0.34 | -0.47 | -1.54 | -3.37 |
| Average <i>total</i> costs (\$K) | | | | | | |
| private | 1043.57 | -24.24 | -1.97 | -2.45 | +11.68 | +63.52 |
| public | 1021.04 | -16.74 | +14.85 | +20.08 | +34.20 | +70.21 |

Conclusion

- We study the procurement with negotiations
 - Develop, identify, and estimate a multiple-agent adverse selection model using the IT/telecommunications procurement contract data
 - Distinguish unilateral vs. bilateral ex-post changes in the contract price and duration
- Key findings:
 - ① Negotiations effectively substitute for one extra bidder
 - ② Government waste is relatively small
 - ③ Less competition for military contracts than nonmilitary ones is driven by the supply side

Contract Price Changes and Contract Type

- Price changes occur *regardless of contract type*

| Fraction of price changes | Firm-fixed | Other |
|---|-------------|-------------|
| In number of contracts | | |
| Unilateral | 0.54 | 0.65 |
| Bilateral | 0.34 | 0.43 |
| In total price (conditional on changes) | | |
| Unilateral | 0.46 (0.35) | 0.45 (0.36) |
| Bilateral | 0.29 (0.28) | 0.32 (0.31) |

Note: Final sample of 962 obs.; standard deviations are in parentheses.

Derivation of π Distribution for Fixed Contracts

- Joint probability that a contract is fixed and $\pi \leq \pi^*$:

$$\begin{aligned} \Pr\{\pi \leq \pi^*, v = 0 | n\} &= F_{\pi|v,n}(\pi^* | 0, n) \Pr(v = 0 | n) \\ &= \int_{\pi=\underline{\pi}}^{\pi^*} f_{\pi|n}(\pi | n) [1 - (1 - \pi)^n] d\pi. \end{aligned}$$

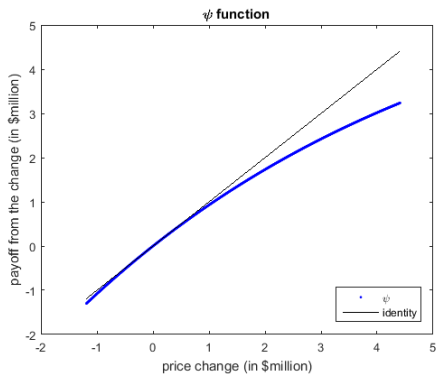
- By taking the first order derivative with respect to π^* :

$$f_{\pi|v,n}(\pi^* | 0, n) \Pr(v = 0 | n) = f_{\pi|n}(\pi^* | n) [1 - (1 - \pi^*)^n].$$

- Note that

$$\Pr(v = 1 | \pi^*, n) = (1 - \pi^*)^n = \frac{f_{\pi|v,n}(\pi^* | 1, n) \Pr(v = 1 | n)}{f_{\pi|n}(\pi^* | n)}$$

Estimates: Liquidity Cost Function

[▶ Back](#)